Computer Science Education in the Montessori Classroom

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Preliminaries

• Slides will be posted at:

- cse4k12.blogspot.com

• Email contact:

- garykac @ either "gmail" or "google" .com

This info will be repeated at end



- Desire to teach computer programming
- Taught class:
 - 6th-8th graders
 - -~40 once-a-week 1-hour classes
 - Student project: create a GBA/NDS game
- First few months of class spent teaching basics
 - These could/should have been taught earlier

Student projects



Why teach computer science?

- Well, why do we:
 - Teach the Bohr model of the atom?
 - Teach photosynthesis?
 - ... other sciences?
- Answer:
 - So students can understand the world around them

Understanding your surroundings

- How does:
 - A toilet work?
 - A phone work?
 - A car (internal combustion engine) work?
- We can explain how these work in general, accessible terms.
 - Concrete physical explanation

How do computers work?

- Many explanations are something like:
 - Mumbling something about 0's and 1's
 - Memory, hard drives, CPU, ALU
- These aren't wrong, but they aren't concrete
 - Students don't walk away with understanding

It's all magic

• "Any sufficiently advanced technology is indistinguishable from magic."

- Arthur C. Clark, 1973

- Kids are growing up in this magical world
- How much of the world will they understand in 20, 30 years?

- Compare this with 100 years ago

But we teach computers, don't we?

- Current state of K-8 computer "science":
 - Typing skills
 - How to use productivity applications
 - Word processing, spreadsheets, ...
- These are necessary, but not sufficient
- We don't teach students how to use a calculator
 - We teach them math

But programming is hard/abstract

- True, so teach programming in 6th-8th
 - Requires abstract thinking
- But teach pre-programming before 6th grade
 - Focus on fundamental principles:
 - Binary
 - Logic
 - Transistors
 - No need for students to use computers for this



- Convince you that teaching pre-programming:
 - Is important
 - Is possible
 - Is easy
 - Well, as easy as any other topic you teach

Pre-programming skills

- Binary / Hexadecimal
- Boolean Logic
- Transistors
- How Computers Add
 - Not a skill per se
 - But useful to tie everything together

Binary / Hexadecimal (3rd-4th grade)

Number systems

• How many ways can you represent a number?

- Tally marks: | || |||
- Roman numerals: LXVII
- Writing systems: 一二三四 ... ١٢٣٤...
- Activity:
 - Grab random number of counters and write the # as many different ways as possible
 - Why: To demonstrate that decimal is not the only way to count things



- The concept of zero is a crucial part of our number system
- Before zero, how do you distinguish between:
 - There were no items
 - Oops, I forgot to fill in this value
- Curriculum link:
 - Compare early societies that invented zero vs. those that didn't

Positional notation

- Decimal is a base-10 positional notation
 - There are 10 digits: 0123456789
 - Value of each digit depends on its position:
 - ..., 1000, 100, 10, 1
 - ..., 10x10x10, 10x10, 10, 1
- Compare 324 and 243
 - Both use same digits
 - Value of each digit is different

Why base-10?

- What about other bases?
 - Some cultures use/used base-5, -12 or -60
- Activity:
 - Where do we see remnants of other bases in modern society?
 - Clocks, Angles, Lat/Long, Eggs
 - Why: Point out that the choice of 10 was somewhat arbitrary

Octal (base-8)

- 8 digits: 01234567
 - Positions: ..., 8x8x8, 8x8, 8, 1
- Why octal?
 - Binary can be confusing at first.
 - Octal is closer to decimal less confusing
- Activity:
 - Get random number of counters. Group by 10 to get decimal. Using same counters, group by 8 to get octal. Repeat.

Counting in octal

- 0, 1, 2, 3, 4, 5, 6, 7, 10, 11, 12, 13, 14, 15, 16, 17, 20, 21, ..., 77, 100, ...
 - 10 comes after 7
 - 20 comes after 17
 - 100 comes after 77
- Compare with decimal
 - 8, 9 are never used

How many is 12?

- Draw 12 circles
 - Ambiguous base-10 or base-8?
- How many circles?
 - 10 (in octal)
 - 8 (in decimal)



Ambiguity

- "12" means different things in octal/decimal
 How do we know which one to use?
- Compare:
 - How do you pronounce "wind"?
 - Is "rose" a noun or a verb?
 - "I'll meet you at 8". Is that AM or PM?
- Context resolves the ambiguity.

Binary (base-2)

- Same as decimal, octal, except:
 - 2 digits: 0, 1
 - Positions: ..., 2x2x2x2, 2x2x2, 2x2, 2, 1

Counting in binary

- 0, 1
 - Oh no, we ran out of digits already
- 10, 11
 - We ran out again
- 100, 101, 110, 111
- 1000, 1001, 1010, 1011, 1100, 1101, 1110, 1111
- This is why we start with octal

Binary activity

• Grab a random number of counters (20-30)

- Group by 2's

- Combine these into groups of 4's
- Repeat into groups of 8's, 16's, 32's
- Place group next to binary position card
- Binary # is created by:
 - Writing a "1" where you have a group
 - Writing a "0" where you don't

Binary activity (example)

• Example, take 11 tokens: 0000000000

- Group by 2: (00)(00)(00)(00)(00)0
- Group by 4: (0000)(0000)(00)0
- Group by 8: (0000000)(00)0
- We have: 1 eight, 0 four, 1 two, 1 one

– Binary number: 1011

Problems with binary

- Decimal is easier to work with
 - 265 versus 100001001
 - What is 11010101101 + 10110100101?
- Non-trivial conversion between base-10

Converting binary/decimal

• Remember, decimal 243 is:

 $-2 \ge 100 + 4 \ge 10 + 3 \ge 1$

• Binary 1011001 is:

-1x64 + 0x32 + 1x16 + 1x8 + 0x4 + 0x2 + 1x1

- = 89

- Ugh! That was work...

Hexadecimal (base-16)

• 16 digits: 0123456789abcdef

- a=10, b=11, c=12, d=13, e=14, f=15
- Single digit representation for each value
- Positions: ..., 16x16x16, 16x16, 16, 1
- Activity: (older students)
 - Where have you seen hexadecimal?
 - Specifying RGB colors: HTML, Photoshop, ...

Counting in hexadecimal

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | а | b | С | d | е | f |
|-----|-----|-----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 1a | 1b | 1c | 1d | 1e | 1f |
| 20 | 21 | 22 | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | |
| e0 | e1 | e2 | e3 | e4 | e5 | e6 | e7 | e8 | e9 | ea | eb | ec | ed | ee | ef |
| fO | f1 | f2 | f3 | f4 | f5 | f6 | f7 | f8 | f9 | fa | fb | fc | fd | fe | ff |
| 100 | 101 | 102 | | | | | | | | | | | | | |

Why hexadecimal?

- Compare positions for binary and hexadecimal
- They line up at 1, 16, 256, ...
- This makes conversion easy

| binary | hexadecimal |
|--------|-------------|
| 1 | 1 |
| 2 | |
| 4 | |
| 8 | |
| 16 | 16 |
| 32 | |
| 64 | |
| 128 | |
| 256 | 256 |
| 512 | |
| 1024 | |
| 2048 | |

Converting binary/hexadecimal

- Binary number: 1110100100100101
- Group by 4 digits: (1110)(1001)(0010)(0101)

- Starting from left side

• Convert each group independently:

| | | | the second s | | | and the second second second | | | | |
|--|--------|-----|--|-----|---|------------------------------|-----|--------|-----|--|
| | binary | hex | binary | hex | | binary | hex | binary | hex | |
| | 0000 | 0 | 0100 | 4 | 1 | 1000 | 8 | 1100 | С | |
| | 0001 | 1 | 0101 | 5 | | 1001 | 9 | 1101 | d | |
| | 0010 | 2 | 0110 | 6 | | 1010 | а | 1110 | е | |
| | 0011 | 3 | 0111 | 7 | | 1011 | b | 1111 | f | |

• Thus, 1110100100100101 becomes E925

Hexadecimal activity

- Activity: Take a set of binary numbers
 - Convert them into *either* decimal or hex
 - Why? Get student to recognize hex is easier
- Extra: (older students)
 - "hexadecimal" is a mix of greek/latin roots
 - It should be "sexadecimal"
 - Compare sexagesimal for base-60
 - Can you guess why hex was chosen?

Boolean Logic (4th-5th grade)

Boolean logic

- Given a set of true/false statements:
 - isRaining true if it's raining outside
 - hasRaincoat true if you have a raincoat
- Formal way of combining statements:
 - getsWet = isRaining AND NOT hasRaincoat
- Basis of logical "thought"
- Two values : true/false. Sounds like binary.
 - -0 =false; 1 =true

Boolean logic activity

- Create logical statements about objects/people in the classroom
 - isRed, isFlat, isBiggerThanMyHead, ...
 - isBoy, hasGreenShirt
- Apply the statements to other objects and state whether they are true or false

Boolean operations

- Four basic operations that can be applied to statements:
 - NOT
 - AND
 - OR
 - XOR
NOT

- Changes true to false and vice versa
- Given
 - isCat = true
- Then

- NOT isCat = false

• In English, we say "is not a cat"

- In logic, we say "not is-a-cat"

AND

- a AND b is true only if a and b are both true
- Given statements:
 - isCat
 - hasStripes
- Then
 - isCat AND hasStripes
 - is true for striped cats
 - is false for spotted cats or striped dogs

OR

- a OR b is true if either a or b (or both) are true
- Given statements:
 - isCat
 - hasStripes
- Then
 - isCat OR hasStripes
 - is true for striped cats, spotted cats, striped dogs
 - is false for spotted dogs

XOR

- **a** XOR **b** is true if either **a** or **b** (but not both) are true
- Given statements:
 - isCat
 - hasStripes
- Then
 - isCat XOR hasStripes
 - is true for spotted cats, striped dogs
 - is false for striped cats, spotted dogs

Boolean logic activity

- Activity #1:
 - Create more logical statements using NOT, OR, AND, XOR
- Activity #2:
 - Take a collection of objects:
 - Items in room, cards from "Guess Who?", ...
 - Choose a few of the objects
 - Create a statement that will be true only for those objects and false for all others

Boolean logic example

- Cockatrice in the game Nethack
 - Petrifies you (turns you to stone) if you touch it
- Logic from game:
 - petrify = (handAttack AND NOT wearGloves) OR (kick AND NOT wearBoots OR (headbutt AND NOT wearHelmet) OR (hug AND NOT (wearGloves AND wearCloak)) OR bite OR sting OR suckBrain OR swallow
 - Note that in the game you can polymorph into monsters (like mind-flayer) that have special attacks (like brain-suck)

Boolean logic activity

- Design a simple game that contains a special object.
 - Create logical expressions that define all the interactions with that object
 - pickUp, drop (on ground, in water), eat, hit, ...
- Trade with a student and see if they can come up with conditions you didn't think of
- Do the same thing for an object in a video game that you've played

Boolean logic – final notes

- Two final notes on boolean logic:
- Truth tables
 - Used to summaries logic statements
 - Useful when solving logic problems
- Logic gates
 - Graphical representation of logical operations

Truth tables

Way of presenting logical statements
 Enumerating all possible outcomes

| isCat | hasStripes | lsCat AND hasStripes | IsCat OR hasStripes | IsCat XOR hasStripes |
|-------|------------|-----------------------------------|----------------------------------|-----------------------------------|
| F | F | F | F | F |
| F | Т | F | Т | Т |
| Т | F | F | т | т |
| Т | Т | Т | Т | F |

Logic gates



Logic gate activity

• Draw one of your logical statements from before as a connected series of gates:



Transistors (4th-5th grade)

Activity

- Good time to cover/review basic electricity:
 - Light bulbs, switches, batteries
 - Electrical current, electrons
 - Materials: conductors vs. insulators
- No need to cover resistors or anything more complex

Binary values in electricity

- Electronic devices typically have 2 electrical states:
 - Power (red wire)
 - Ground (black wire)
 - For a battery: (-) Ground (+) Power
- Two states. Sounds like binary:
 - -0 =Ground; 1 =Power

Transistors

- What are transistors?
 - Electrical switches
- Similar to the light switches:
 - Two positions: on / off
 - On: electricity flows to lightbulb
 - Off: electricity does not flow to lightbulb
 - Difference:
 - Switch is controlled electrically
 - So a switch can control another switch

Transistor

Α

В



If switch is ON A and B are connected

If switch is OFF A and B are not connected Types of transistors

- Lots of different types:
 - FET : field effect transistor
 - BJT : bipolar junction transistor
- But we don't care:
 - Just pick one that is easy to explain:
 - MOSFETs : metal oxide semiconductor FET
 - Also one of the more common types

Semiconductors

- Semiconductors:
 - Not good conductors
 - Not good insulators
- What good are they?
 - With the right tricks, they can switch from one state to the other
 - This is how transistors work

CMOS

• CMOS (complementary MOS):

- Uses nMOS and pMOS transistors
- Arranged in a complementary fashion



Building logic gates from transistors

- Invertor (boolean NOT) is the simplest
 - Requires 2 transistors: 1 nMOS & 1 pMOS
- Other gates can be built with 2 of each type:
 - NAND = NOT AND
 - NOR = NOT OR
- We can combine gates:
 - AND = NOT NAND
 - OR = NOT NOR



Transistor activity - inverter

- Use cards to build logic gates from transistors
- Red/black markers for power/ground
- Students trace flow of "0"s and "1"s



How Computers Add (5th-6th grade)

How computers add

Computers add the same way humans add
Except in binary

How do you teach addition?

| | | | | | | E | 3 | | | | |
|-----|---|---|----|----|----|----|----|----|----|----|----|
| | + | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 100 | 0 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| | 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| | 2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| | 3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| | 4 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| | 5 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| | 6 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| | 7 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| | 8 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| | 9 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |

Memorize this table!

Teaching addition (review)

• First teach adding 2 single-digit numbers

- 1+1=2, 3+5=8, ...

- Later, multi-digit answers:

• 7+8 = 15

• Then expand to adding multi-digit numbers:

-18+23=41

- With carry

Single digit addition





carry sum

Add the 2 blue numbers

Produce the single-digit sum (green) and the carry (yellow)

Sum table & carry table

| | | | | | E | 3 | | | | |
|---|---|---|---|---|---|---|---|---|---|---|
| + | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 1 |
| 3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 1 | 2 |
| 4 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 1 | 2 | 3 |
| 5 | 5 | 6 | 7 | 8 | 9 | 0 | 1 | 2 | 3 | 4 |
| 6 | 6 | 7 | 8 | 9 | 0 | 1 | 2 | 3 | 4 | 5 |
| 7 | 7 | 8 | 9 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| 8 | 8 | 9 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 9 | 9 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

Sum table

А

Carry table

| | 6.12 | в | | | | | | | | | |
|---|------|---|---|---|---|---|---|---|---|---|---|
| | + | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| | 4 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| | 5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 |
| | 6 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 7 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 8 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 9 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

Binary addition

- Same general idea as with decimal
- Uses binary addition table
 - Just like the decimal addition table

Binary addition table

| | | E | 3 |
|---|---|---|----|
| | + | 0 | 1 |
| ٨ | 0 | 0 | 1 |
| A | 1 | 1 | 10 |

That's all

Binary sum and carry tables

• Binary addition table:



• As before, break into sum and carry tables:



More logically...

Re-writing these 2 tables more "logically"



| Wa got. | 1.1.2.1.2.1.2.1 | No. Sons. | | |
|---------|-----------------|-----------|-------|-----|
| we get. | Α | В | Carry | Sum |
| | 0 | 0 | 0 | 0 |
| | 0 | 1 | 0 | 1 |
| | 1 | 0 | 0 | 1 |
| | 1 | 1 | 1 | 0 |

Adding with logic gates

Compare this with our boolean logic gates:

| Α | В | Carry | Sum | AND | XOR |
|---|---|-------|-----|-----|-----|
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 | 1 | 0 |

Carry is AND

Sum is XOR



Half-adder activity

- Use cards like with the transistor
 - AND, XOR gate cards + yarn for "wire"
- Build a half-adder
- Verify that it produces the binary addition table

Adding multiple digits

- A half-adder only adds 2 single digit numbers
 It only does "half" the job
- We need to be able to handle both carries
 - Carry coming in from previous digit
 - Carry going out to next digit
Multi-digit addition (decimal)



Add the 3 blue numbers

Produce the 2 green numbers

Supporting carries with a full-adder

- A full-adder extends the half-adder by adding support for the carry
- Two steps:
 - Add the two numbers (as before)
 - Add the carry to the result
- Built from 2 half-adders
 - Plus an OR gate to combine the carries

Full-adder



1.2.0.00

Full-adder activity

- Using cards, construct a full-adder and verify it works
- Investigate why we can OR the carries together
 - Each half-adder produces a carry
 - The full-adder just ORs the 2 carries together
 - Is it possible for both carries to be set at the same time?

Ripple carry adder

- Full adders connected together
 - Propagate the carry from one digit to the next
 - Just like we teach students to do for decimal
- Any number of full adders can be connected
 - 4 full adders supports adding two 4-digit numbers

Ripple carry adder



Ripple carry adder activity

- With N students, give each one a full-adder to construct.
 - Connect them end-to-end to build a ripple carry adder
 - Add 2 N-digit binary numbers

Resources

- Slides will be posted at:
 - cse4k12.blogspot.com
 - Updates will also be posted there
- We are in the process of converting these activities into worksheets/activity sheets.
- Email contact:
 - garykac @ either "gmail" or "google" .com